



DETAILED EVALUATION OF CFD PREDICTIONS AGAINST LDA MEASUREMENTS FOR FLOW ON AN AEROFOIL

**A. Benyahia ¹, E. Berton ¹, D. Favier ¹, C. Maresca ¹, K. J. Badcock ²,
G.N.Barakos ²**

*1 L.A.B.M., Laboratoire d'Aérodynamique et de Biomécanique du Mouvement,
UMSR 2164 of CNRS and University of Méditerranée,
163 Avenue de Luminy, case 918, 13288 Marseille Cedex 09, France*

2 University of Glasgow, Department of Aerospace Engineering? Glasgow G12 8QQ, U.K



Presentation Outline

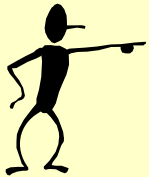
- Introduction and objectives
- Experimental methodology: LDV measurements
- Numerical methodology: PMB approach
- Results and discussion
- Conclusions and prospects

Introduction and objectives

- The detailed knowledge of the boundary-layer response to unsteadiness induced by oscillating models is of major interest in a wide range of aeronautical applications.
- This work concerns an experimental and numerical investigation of the unsteady boundary-layer on a NACA0012 aerofoil oscillating in pitching motion.
- The experimental part of the present study is based on the Embedded Laser Doppler Velocimetry, developed at LABM for unsteady boundary-layer investigation.
- From the numerical point of view, simulations were performed using the PMB solver developed at GU based on a RANS approach of turbulence.

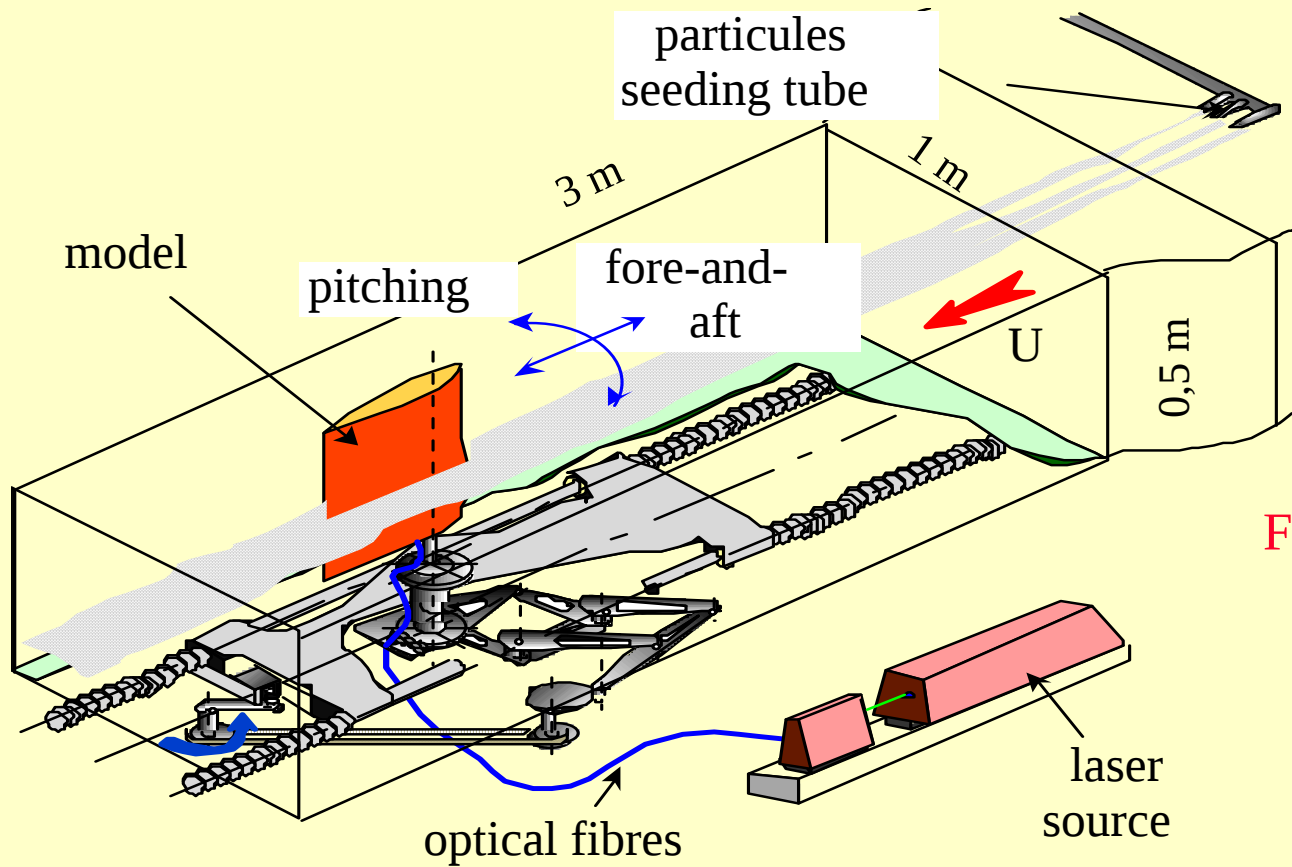
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- Introduction and objectives

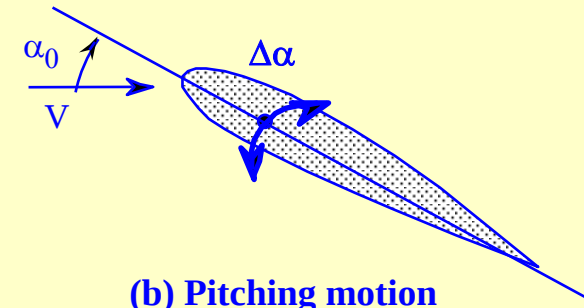


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S2 Luminy wind-tunnel-Experimental Set-up



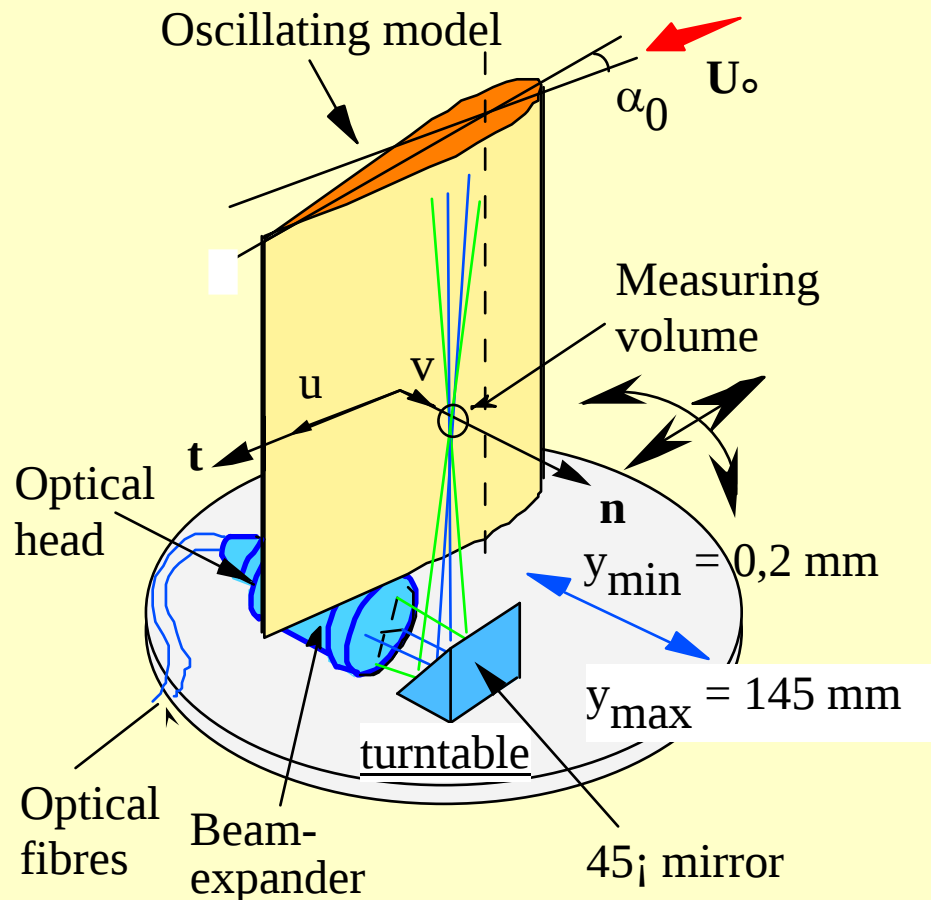
Forced unsteadiness law



(b) Pitching motion

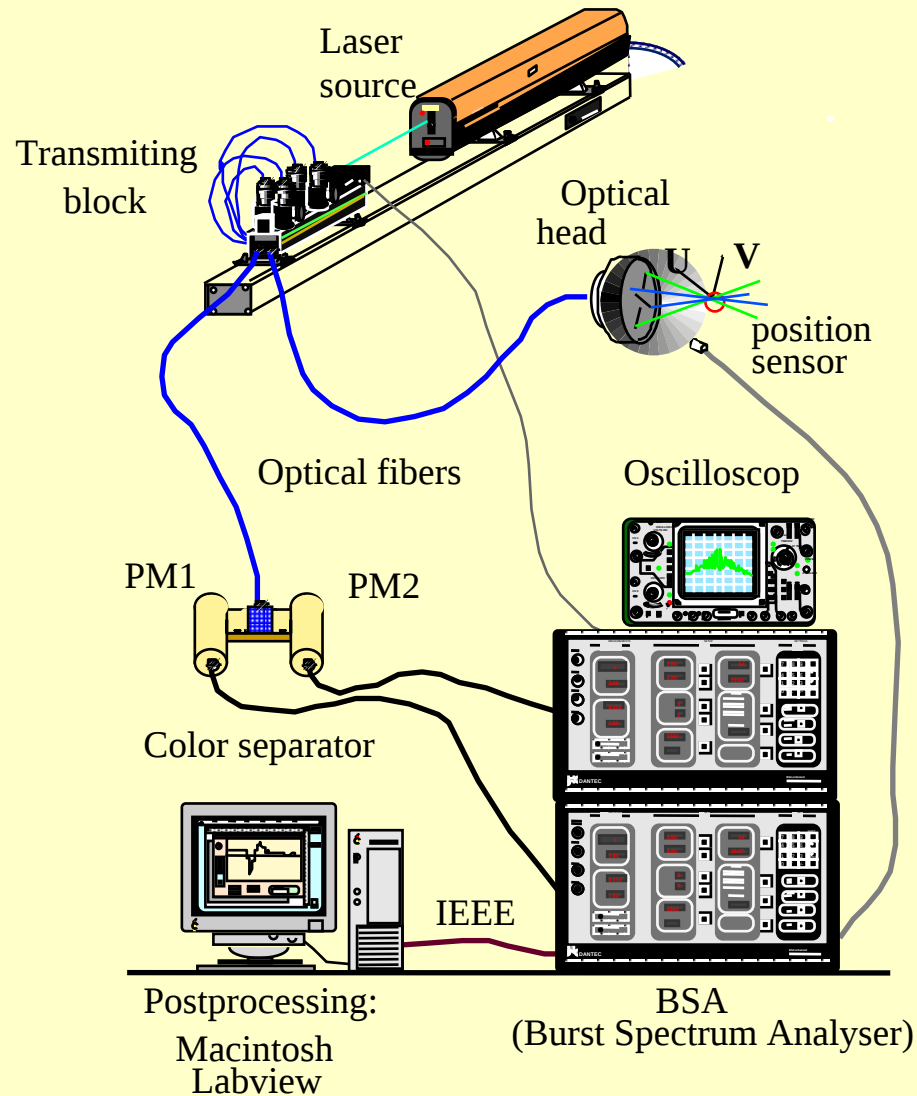
$$\alpha(t) = \alpha_0 + \Delta\alpha \cos(\omega t)$$

Embedded Laser Doppler Velocimetry Method (ELDV)

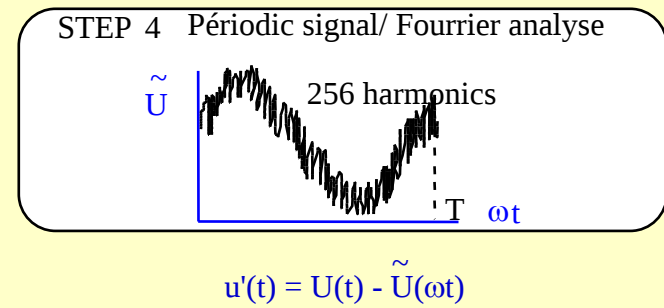
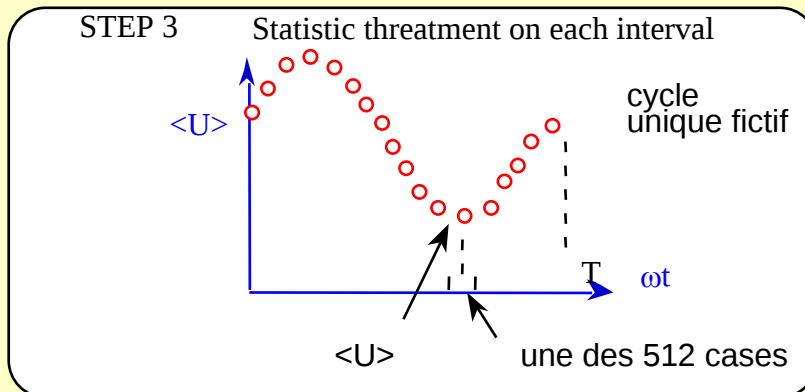
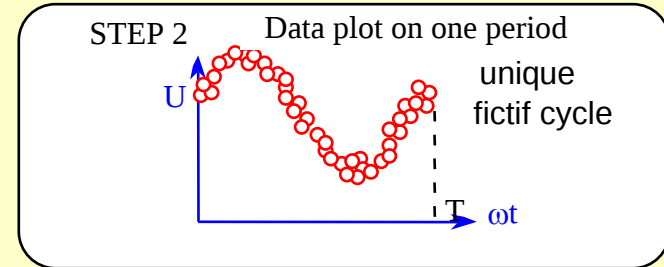
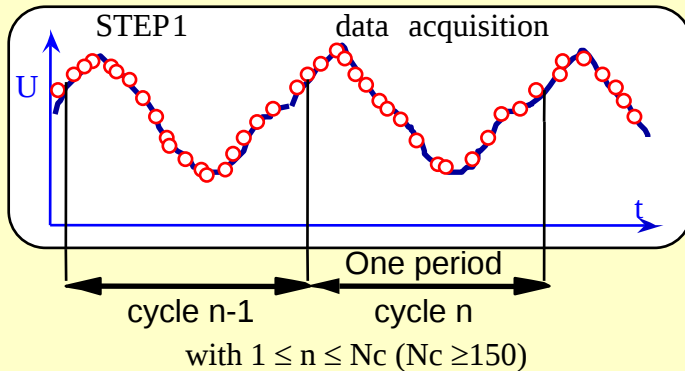


- Embedded optical head linked with the model
- Reference frame linked with the moving surface
- Focal length $f = 400 \text{ mm}$
- Survey along the chord (x direction)
- Survey along the normal (y direction)

ELDV Acquisition



Unsteady measurements processing



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Parallel Multi-Block (PMB) : RANS approach for the turbulence

PMB RANS approach principle

- Transport equations

$$\frac{\partial W}{\partial t} + \frac{\partial (F^i - F^v)}{\partial x} + \frac{\partial (G^i - G^v)}{\partial y} = 0$$

$$W = (\rho, \rho u, \rho v, \rho e_T)$$

$$F^i = (\rho u, \rho u^2 + p, \rho uv, \rho uh)$$

$$G^i = (\rho u, \rho uv, \rho v^2 + p, \rho vh)$$

$$F^v = \frac{1}{\text{Re}} (0, \tau_{xx}, \tau_{xy}, u\tau_{xx} + v\tau_{yy} + q_x) \quad G^v = \frac{1}{\text{Re}} (0, \tau_{xy}, \tau_{yy}, u\tau_{xy} + v\tau_{yy} + q_y)$$

$$\tau_{xx} = -(\mu + \mu_T) \left(2 \frac{\partial u}{\partial x} - \frac{2}{3} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \right) + \frac{2}{3} \rho k \quad \tau_{yy} = -(\mu + \mu_T) \left(2 \frac{\partial v}{\partial y} - \frac{2}{3} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) \right) + \frac{2}{3} \rho k$$

$$\tau_{xy} = -(\mu + \mu_T) \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right)$$

PMB RANS approach principle

- The resolution method

Implicite scheme :

$$\frac{W_{i,j,k}^{n+1} - W_{i,j,k}^n}{\Delta t} = -\frac{1}{V_{i,j,k}} R_{i,j,k} (W_{i,j,k}^{n+1})$$

Turbulence models: 1 or 2 equations models. Spalart-Allmaras (SA), $k-\omega$ et SST.

$$\rho = \bar{\rho} + \rho' \quad p = \bar{p} + p' \quad u = \bar{u} + u' \quad v = \bar{v} + v'$$

PMB RANS approach principle

- Le modèle SA

$$\nu_T = \tilde{\nu} f_{v1}$$

$$f_{v1} = \frac{\chi^3}{\chi^3 + c_{v1}^3} \quad \chi \equiv \frac{\tilde{\nu}}{\nu}$$

$$\frac{D\tilde{\nu}}{Dt} = c_{b1} \tilde{S} \tilde{\nu} + \frac{1}{\sigma} \left[\nabla \cdot ((\nu + \tilde{\nu}) \nabla \tilde{\nu}) + c_{b2} (\nabla \tilde{\nu})^2 \right] - c_{\omega1} f_{\omega} \left[\frac{\tilde{\nu}}{d} \right]^2$$

$$\tilde{S} \equiv S + \frac{\tilde{\nu}}{\kappa^2 d^2} f_{v2} \quad f_{v2} = 1 - \frac{\chi}{1 + \chi f_{v1}} \quad f_{\omega} = g \left[\frac{1 + c_{\omega3}^6}{g^6 + c_{\omega3}^6} \right]^{1/6} \quad g = r + c_{\omega2} (r^6 - r) \quad r \equiv \frac{\tilde{\nu}}{\tilde{S} \kappa^2 d^2}$$

$$c_{b1} = 0.135 \quad \sigma = 2/3 \quad c_{b2} = 0.622 \quad \kappa = 0.41 \quad c_{\omega1} = 2.762 \quad c_{\omega2} = 0.3 \quad c_{\omega3} = 2 \quad c_{v1} = 7.1$$

PMB RANS approach principle

- Le modèle k- ω

$$\mu_T = \rho k / \omega$$

$$\rho \frac{\partial k}{\partial t} + \rho V \cdot \nabla k - \frac{1}{\text{Re}} \nabla \cdot [(\mu + \sigma^* \mu_T) \nabla k] = P_k - \beta^* \rho k \omega$$

$$\rho \frac{\partial \omega}{\partial t} + \rho V \cdot \nabla \omega - \frac{1}{\text{Re}} \nabla \cdot [(\mu + \sigma \mu_T) \nabla \omega] = P_\omega - \beta \rho k \omega^2$$

$$\alpha = 5/9$$

$$\beta = 3/40$$

$$\beta^* = 9/100$$

$$\sigma = 1/2$$

$$\sigma^* = 1/2$$

PMB RANS approach principle

- Le modèle de transport du tenseur visqueux (SST)

$$\mu_T = \frac{\rho k / \omega}{\max[1; \Omega F_2 / (a_1 \omega)]}$$

$$F_2 = \tanh \left[\left(\max \left[2 \frac{\sqrt{k}}{0.09 \omega y}; \frac{500 \mu}{\rho y^2 \omega} \right] \right)^2 \right]$$

$$\rho \frac{\partial k}{\partial t} + \rho V \cdot \nabla k - \frac{1}{\text{Re}} \nabla \cdot [(\mu + \sigma^* \mu_T) \nabla k] = P_k - \beta^* \rho k \omega$$

$$\rho \frac{\partial \omega}{\partial t} + \rho V \cdot \nabla \omega - \frac{1}{\text{Re}} \nabla \cdot [(\mu + \sigma_{\omega 1} \mu_T) \nabla \omega] = P_\omega - \beta \rho k \omega^2 + 2(1 - F_1) \frac{\rho \sigma_{\omega 2}}{\omega} \nabla k \nabla \omega$$

$$F_1 = \tanh \left[\left[\min \left(\max \left[\frac{\sqrt{k}}{0.09 \omega y}; \frac{500 \mu}{\rho y^2 \omega} \right]; \frac{4 \rho \sigma_{\omega 2} k}{CD_{k\omega} y^2} \right) \right]^4 \right]$$

$$CD_{k\omega} = \max \left[\frac{2 \rho \sigma_{\omega 2}}{\omega} \nabla k \nabla \omega; 10^{-20} \right]$$

$$a_1 = 0.31$$

$$\beta^* = 0.09$$

$$\kappa = 0.41$$



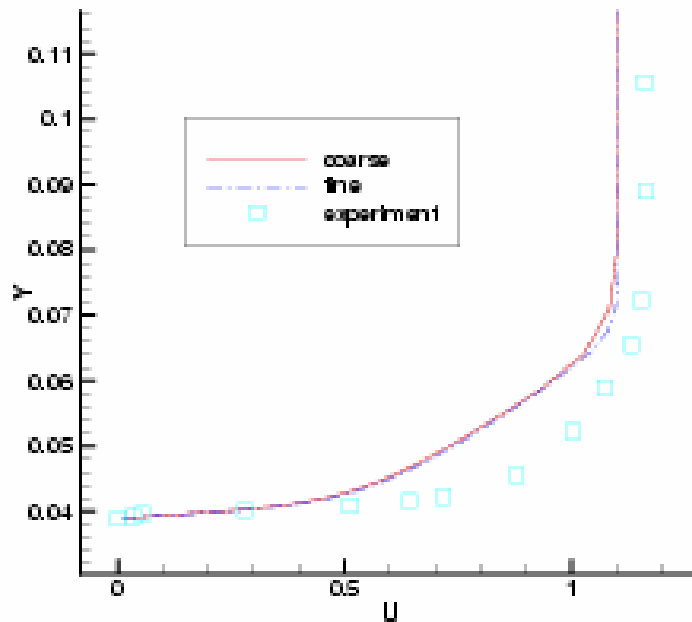
Results

Presentation Outline

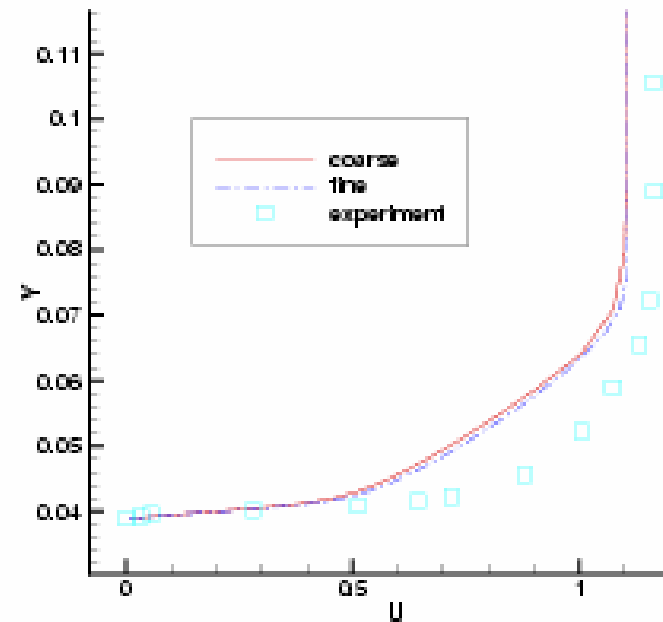
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2 meshes results



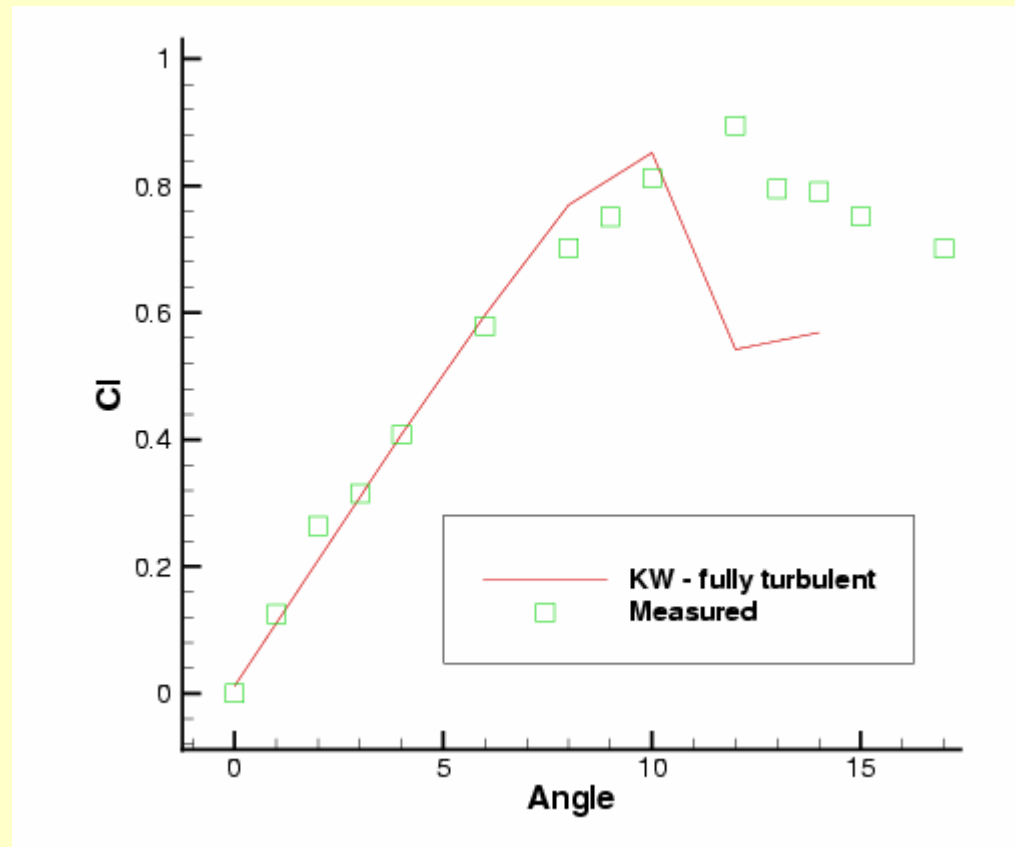
KW model



SA model

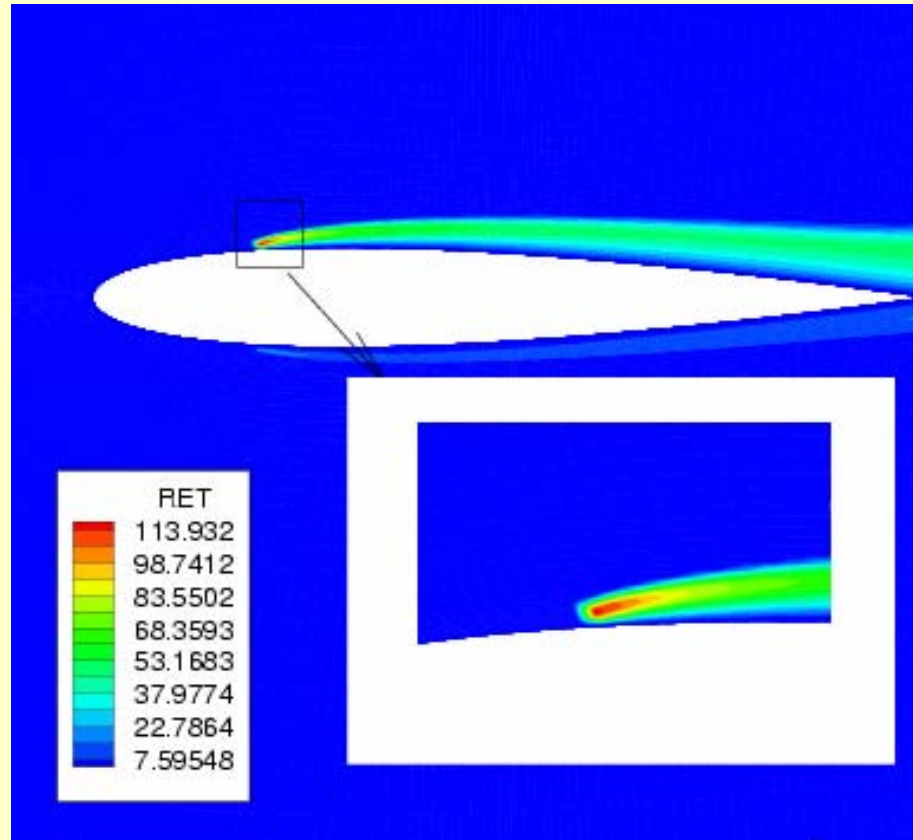
Fine mesh, 27501 points
Coarse mesh, 6975 points

Lift coefficient



Fixed incidence case

Turbulence Reynolds Number

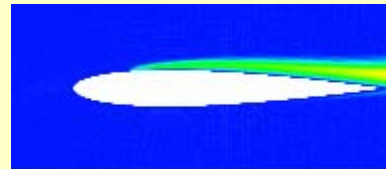


$k-\omega$ model with imposed transition at $s/c=0.2$

Turbulence Reynolds Number



KW - fully turbulent



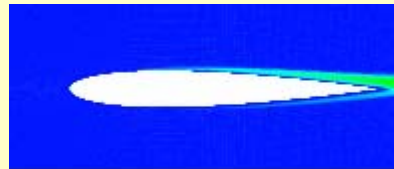
KW - method 2(0.2)



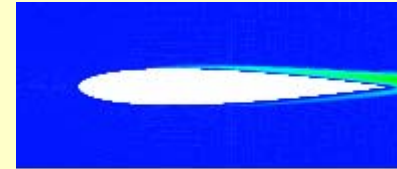
KW - method 2(0.1-0.3)



SA - fully turbulent



SA - method 2(0.2)



SA - method 2(0.1-0.3)



SST - fully turbulent



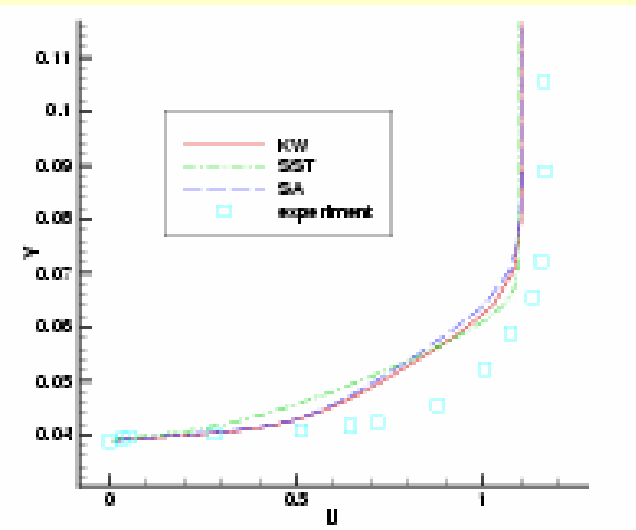
SST - method 2(0.2)



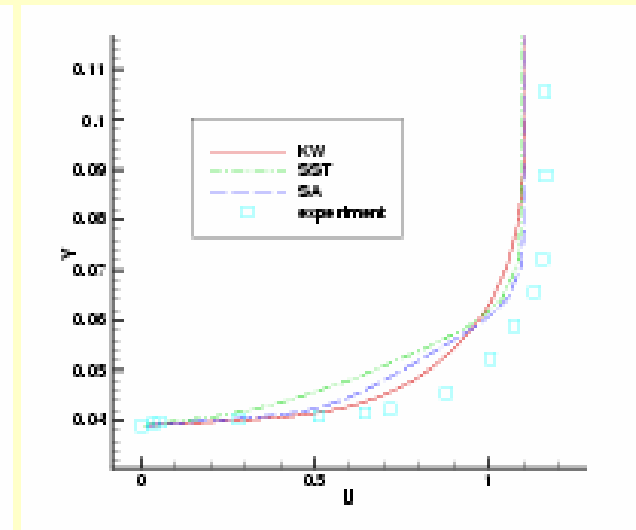
SST - method 2(0.1-0.3)

Différents model with or without transition

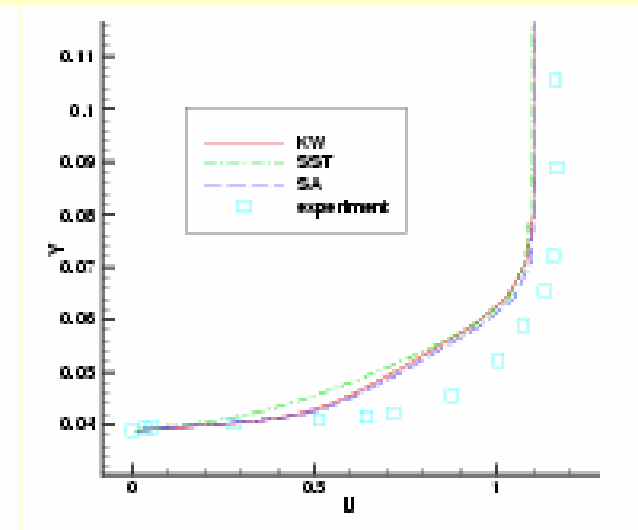
Velocity Profiles



Fully turbulent

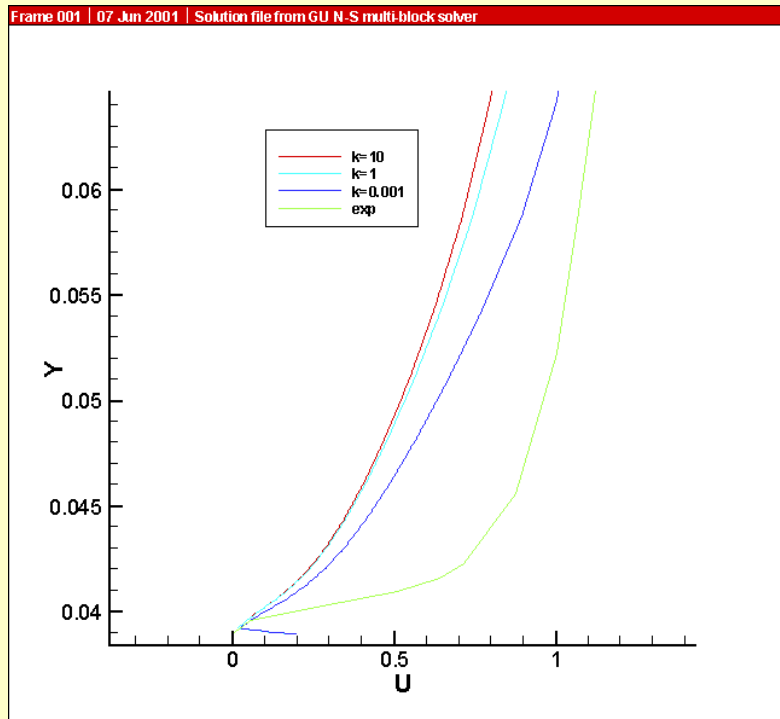


Transition fixed at $s/c=0.2$

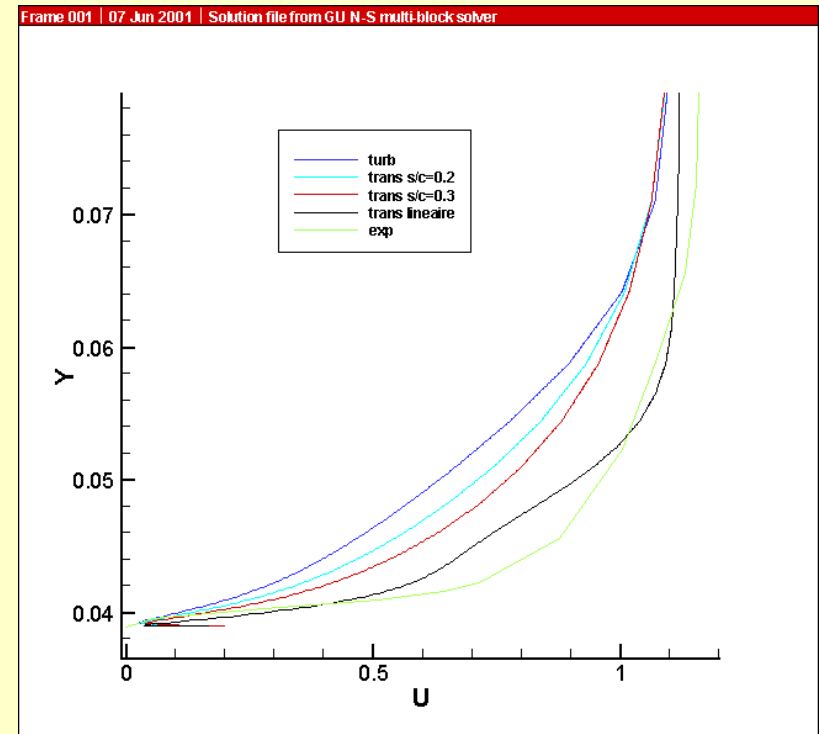


Transition increasing
linearly between $s/c=0.1$
and $s/c=0.3$

Velocity Profiles

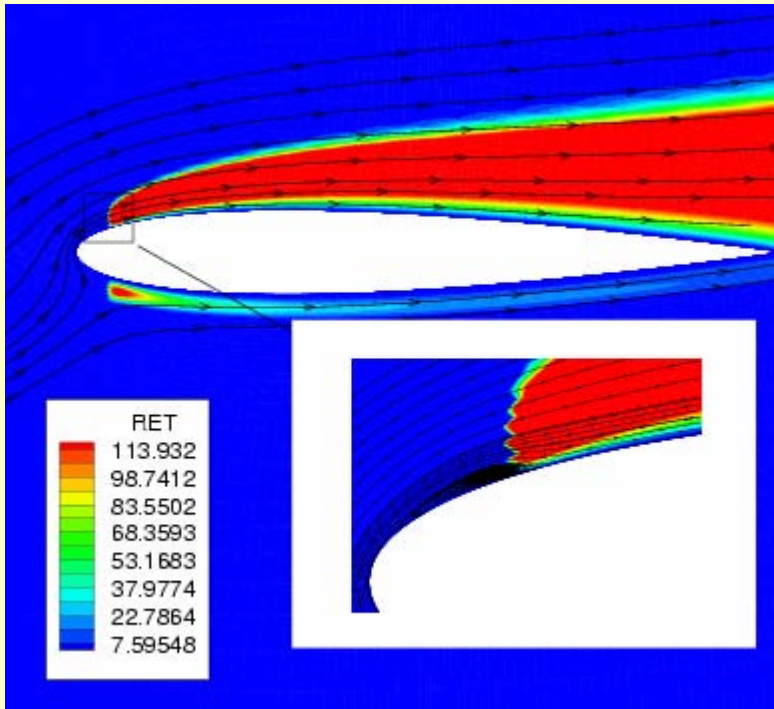


SST model for different values of k

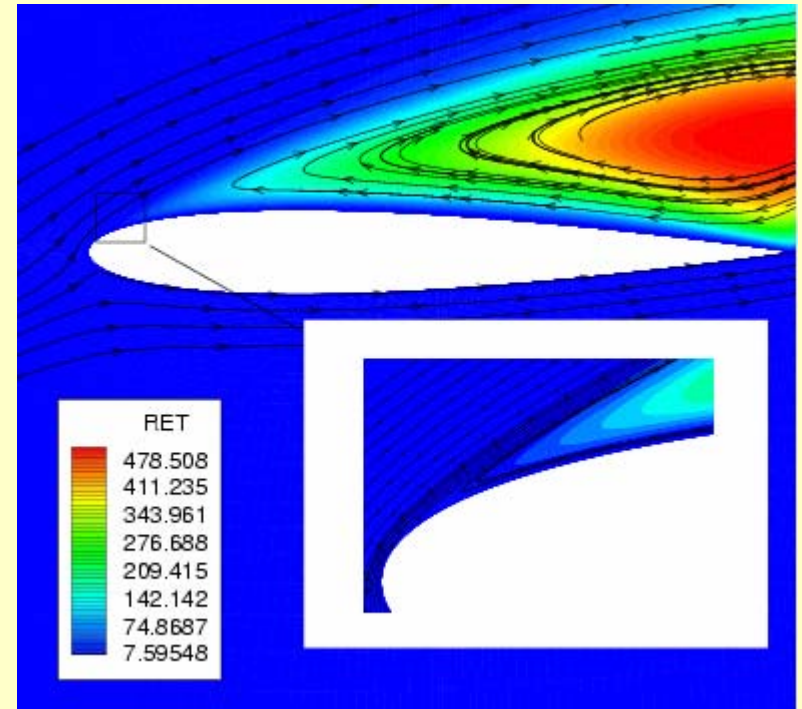


SST models for different transition localisations and $k=0.001$

Turbulence Reynolds Number

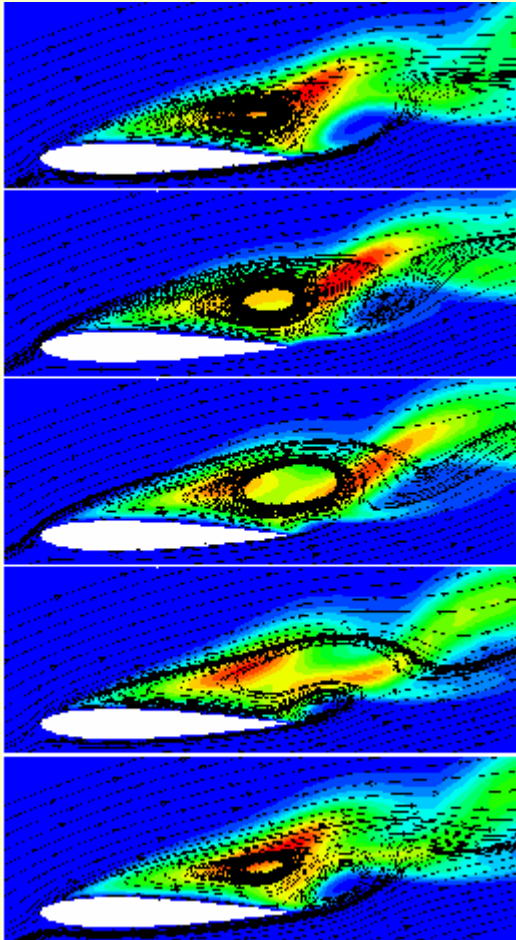


$\alpha=15$ deg: SST model with
transition fixed at $s/c=0.05$



$\alpha=15$ deg: SST model fully
turbulent

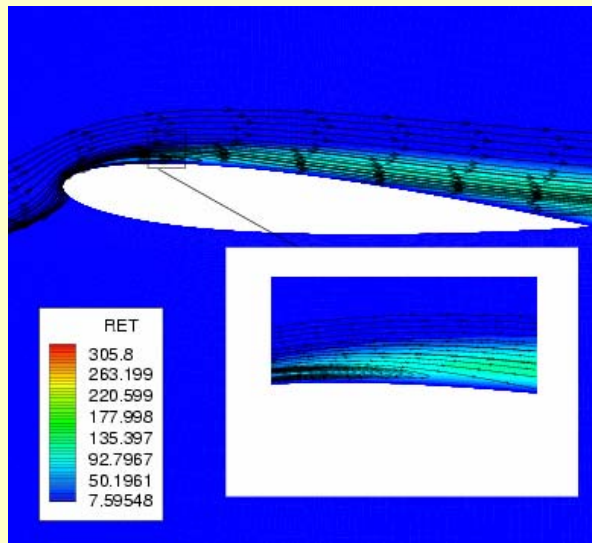
Turbulence Reynolds Number



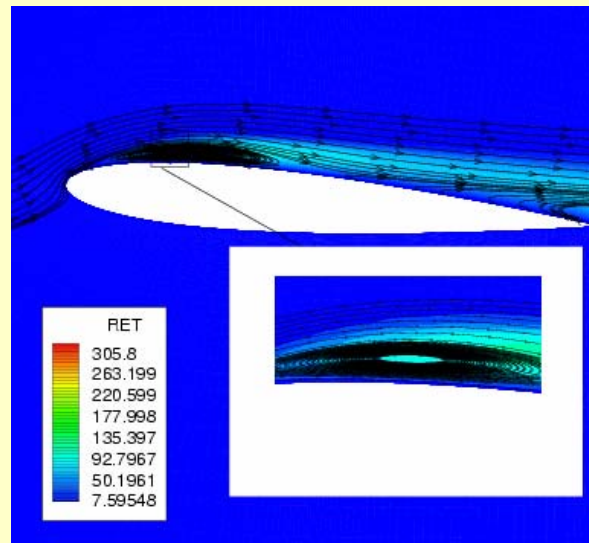
Vortex shedding with a characteristic dimensionless frequency of $k = 0.51$

Turbulence Reynolds Number

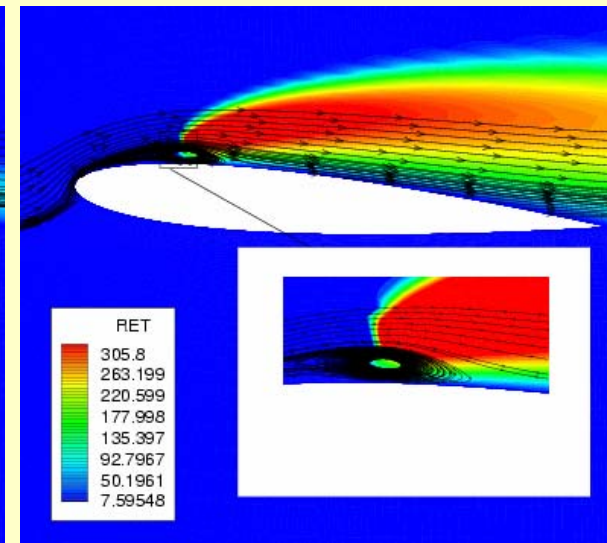
Pitching motion, $\alpha(t) = \alpha_0 + \Delta\alpha \cos(\omega t)$
 $\alpha_0 = 6^\circ$, $\Delta\alpha = 6^\circ$, $k = \omega c / 2U_\infty = 0.188$



12°: k- ω model fully
turbulent



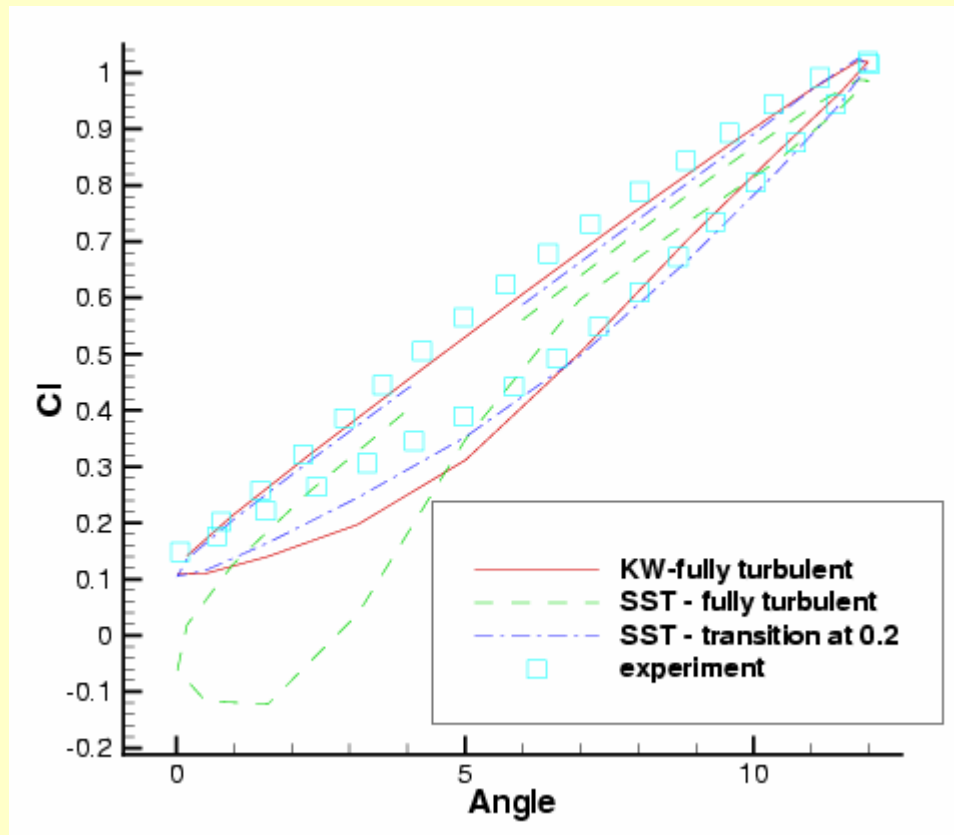
12°: SST model fully
turbulent



12°: SST model with
transition location at $s/c=0.2$

Lift coefficient

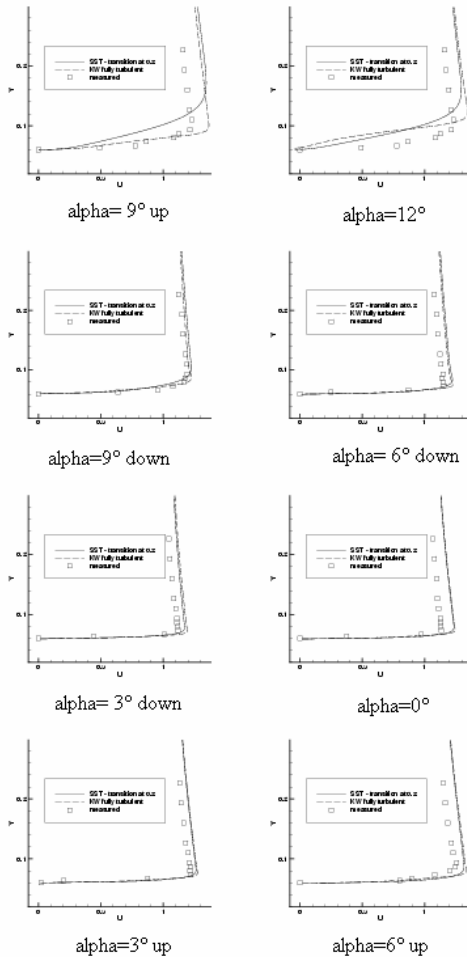
Pitching motion, $\alpha(t) = \alpha_0 + \Delta\alpha \cos(\omega t)$
 $\alpha_0 = 6^\circ$, $\Delta\alpha = 6^\circ$, $k = \omega c / 2U_\infty = 0.188$



Hysteresis loops

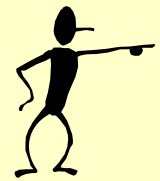
Velocity Profiles

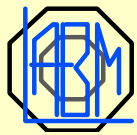
SST model with transition
located at $s/c=0.2$ and $k-\omega$
model fully turbulent



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Conclusions

- Using such ELDV measurement methods, the boundary-layer behaviour can be fully investigated and characterized in a moving frame of reference.
- Analysis of the effects of forced unsteadiness (due to the pitching motion) on B.L.
- Dependence on turbulence model and transition
- Better agreement with experiment for transitionnal models for static incidence, before stall. Fully turbulent models are more adapted for oscillation case