

IDENTIFICATION OF STRUCTURAL DAMPING FROM TESTS

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- Energy balance identification method
- Validation (Numerical simulation / Experiments)
- Future and current work

Objectives of the research

Main sources of energy dissipation in a structure

- Joints (bolts, rivets, welding, supports, bearings, ...)
- Material damping (electronic mechanisms, dislocations, relaxation on grain boundaries, irreversible intercrystal heat flux, thermoelastic damping, thermal hysteresis, eddy currents, ferromagnetic hysteresis, ...)

Objectives of the research

$$\mathbf{M}\ddot{\mathbf{x}} + \mathbf{C}\dot{\mathbf{x}} + \mathbf{K}\mathbf{x} = \mathbf{f}(t)$$



Inertia
forces



Viscous
damping



Elastic
forces



External
forces

Issues in damping identification

- Simplified mathematical model needed
- Computational time
- Incompleteness of data (modal and spatial)
- Generally small effect on dynamics, difficult measurement

Modal and spatial identification

Modal identification:

Modal damping ratio ζ_i

Loss factor η_i

- Logarithmic decrement
- Half-power bandwidth method

Modal and spatial identification

Spatial identification:

Viscous damping matrix \mathbf{C}

- Modal parameters λ_n, Ψ_n
(Perturbation methods, Lancaster's formula, ...)
- Frequency Response Function $\mathbf{H}(\omega)$
(Imaginary part of dynamic stiffness matrix, ...)
- Time history $\mathbf{x}(t), \dot{\mathbf{x}}(t), \ddot{\mathbf{x}}(t)$
(Energy balance method, ...)

Advantages of the energy approach

- Good performance when noise and/or modal incompleteness is present.
- Potential identification of nonlinear damping.
- System model not needed under certain assumptions.

Theory

The new method is based on the energy balance method, starting from the equations of motion of a MDOF system

$$\mathbf{M}\ddot{\mathbf{x}} + \mathbf{D} g(\mathbf{x}, \dot{\mathbf{x}}) + \mathbf{K}\mathbf{x} = \mathbf{f}(t)$$

The energy equation can be derived

$$\int_t^{t+T_1} \dot{\mathbf{x}}^T (\mathbf{M}\ddot{\mathbf{x}} + \mathbf{D} g(\mathbf{x}, \dot{\mathbf{x}}) + \mathbf{K}\mathbf{x}) dt = \int_t^{t+T_1} \dot{\mathbf{x}}^T \mathbf{f}(t) dt$$

Theory

In the case of periodic response, the contribution of conservative forces to the total energy over a full cycle of periodic motion is zero. So if $T_I = T$ (period of the response)

$$\int_t^{t+T} \dot{\mathbf{x}}^T (\mathbf{M}\ddot{\mathbf{x}} + \mathbf{K}\mathbf{x}) dt = 0$$

And the energy equation can be reduced to

$$\int_t^{t+T} \dot{\mathbf{x}}^T \mathbf{D} g(\mathbf{x}, \dot{\mathbf{x}}) dt = \int_t^{t+T} \dot{\mathbf{x}}^T \mathbf{f}(t) dt$$

Solve for \mathbf{D}

Energy equivalent

\mathbf{D}_e

Diagonal viscous damping matrix

$$\mathbf{C} = \begin{bmatrix} c_1 & 0 & \dots & 0 & \dots & 0 \\ 0 & c_2 & \dots & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & 0 & \dots & 0 \\ 0 & 0 & 0 & c_p & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \ddots & 0 \\ 0 & 0 & 0 & 0 & 0 & c_n \end{bmatrix}$$

Diagonal viscous damping matrix

The simplest case is a system with diagonal viscous damping matrix. In this case the energy equation becomes

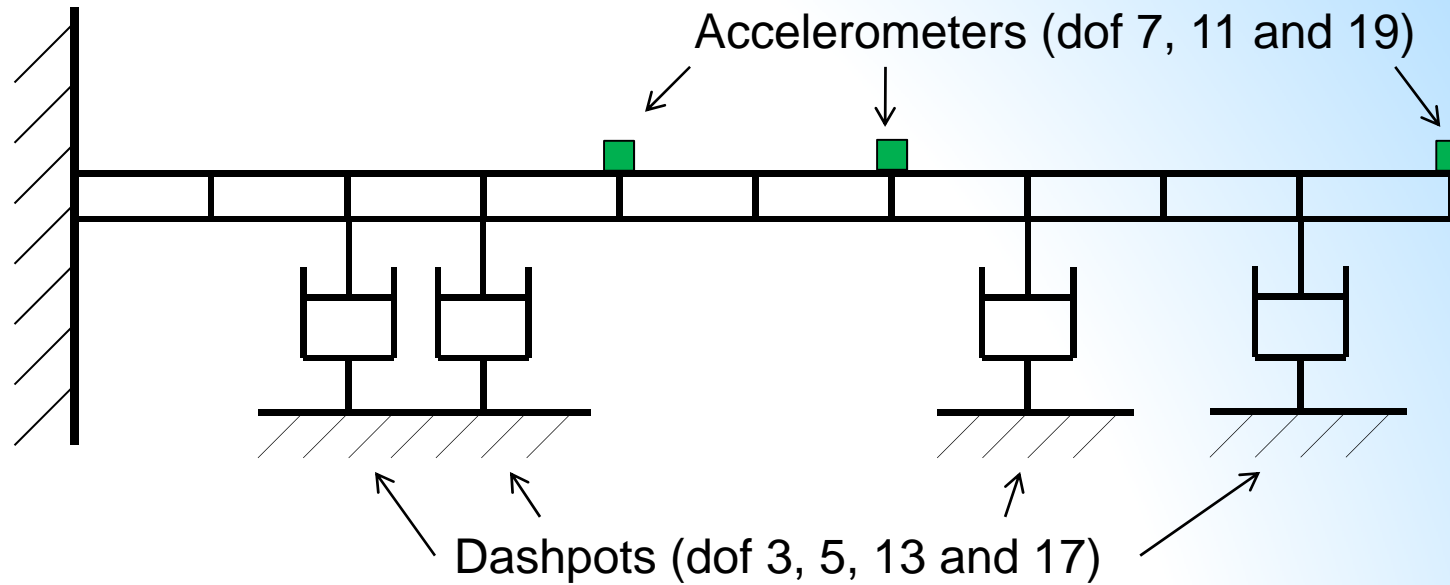
$$\int_t^{t+T} \dot{\mathbf{x}}^T \mathbf{C} \dot{\mathbf{x}} dt = \int_t^{t+T} \dot{\mathbf{x}}^T \mathbf{f}(t) dt$$

$$c_1 \int_t^{t+T} \dot{x}_1^2 dt + c_2 \int_t^{t+T} \dot{x}_2^2 dt + \dots + c_n \int_t^{t+T} \dot{x}_n^2 dt = \int_t^{t+T} \dot{\mathbf{x}}^T \mathbf{f}(t) dt$$

Diagonal viscous damping matrix

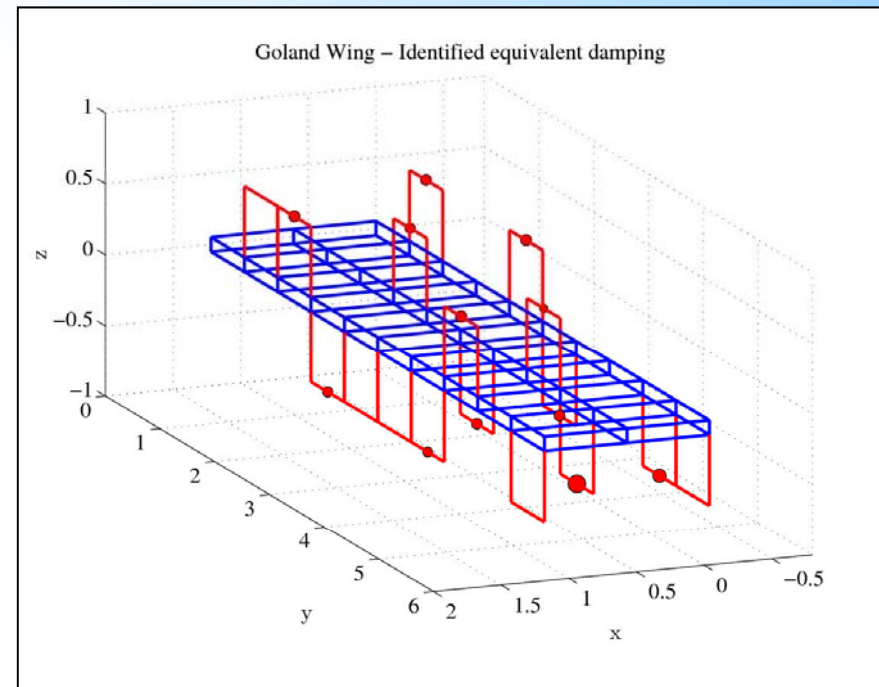
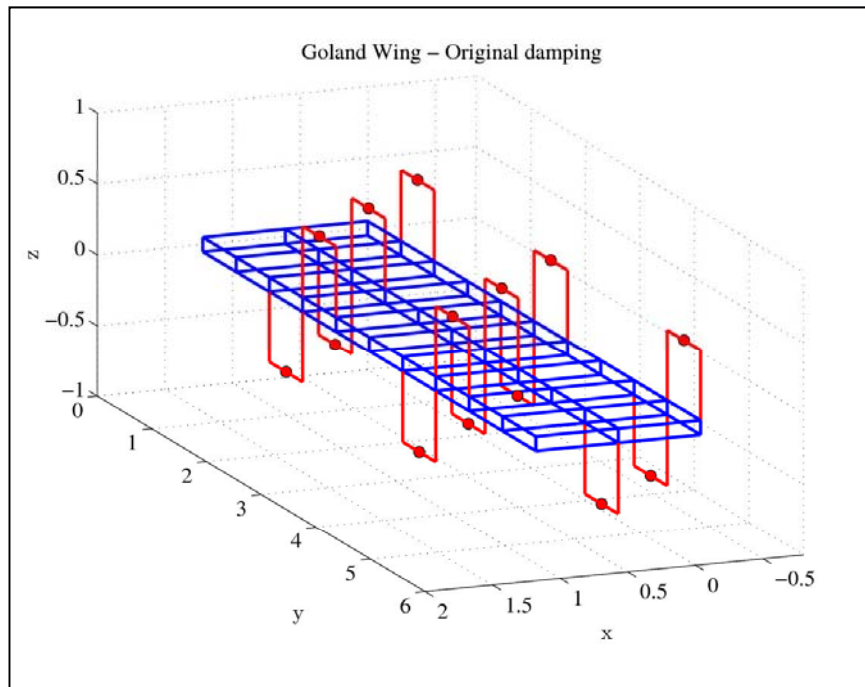
$$\begin{bmatrix} \int_t^{t+T_1} \dot{x}_{1(1)}^2 dt & \int_t^{t+T_1} \dot{x}_{2(1)}^2 dt & \dots & \int_t^{t+T_1} \dot{x}_{n(1)}^2 dt \\ \int_t^{t+T_2} \dot{x}_{1(2)}^2 dt & \int_t^{t+T_2} \dot{x}_{2(2)}^2 dt & \dots & \int_t^{t+T_2} \dot{x}_{n(2)}^2 dt \\ \dots & \dots & \dots & \dots \\ \int_t^{t+T_m} \dot{x}_{1(m)}^2 dt & \int_t^{t+T_m} \dot{x}_{2(m)}^2 dt & \dots & \int_t^{t+T_m} \dot{x}_{n(m)}^2 dt \end{bmatrix} \begin{Bmatrix} C_1 \\ C_2 \\ \dots \\ C_n \end{Bmatrix} = \begin{Bmatrix} \int_t^{t+T_1} \dot{\mathbf{x}}^T \mathbf{f}_1(t) dt \\ \int_t^{t+T_2} \dot{\mathbf{x}}^T \mathbf{f}_2(t) dt \\ \dots \\ \int_t^{t+T_m} \dot{\mathbf{x}}^T \mathbf{f}_m(t) dt \end{Bmatrix}$$

Validation: numerical example

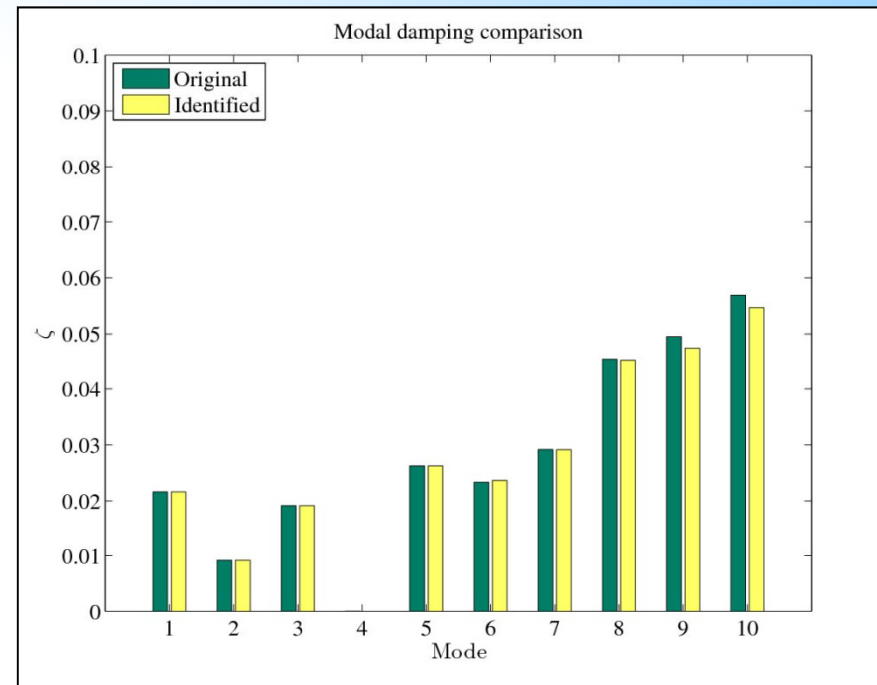
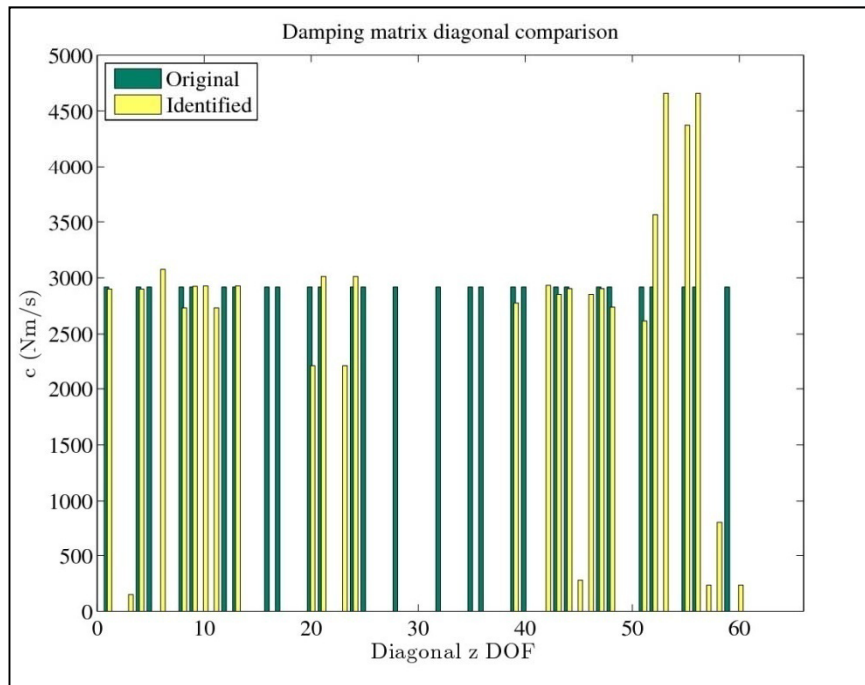


Prandina, M., Mottershead, J.E., and Bonisoli, E., Location and identification of damping parameters, IMAC XXVII Conference and Exposition on Structural Dynamics, Orlando, Florida, USA, 2009.

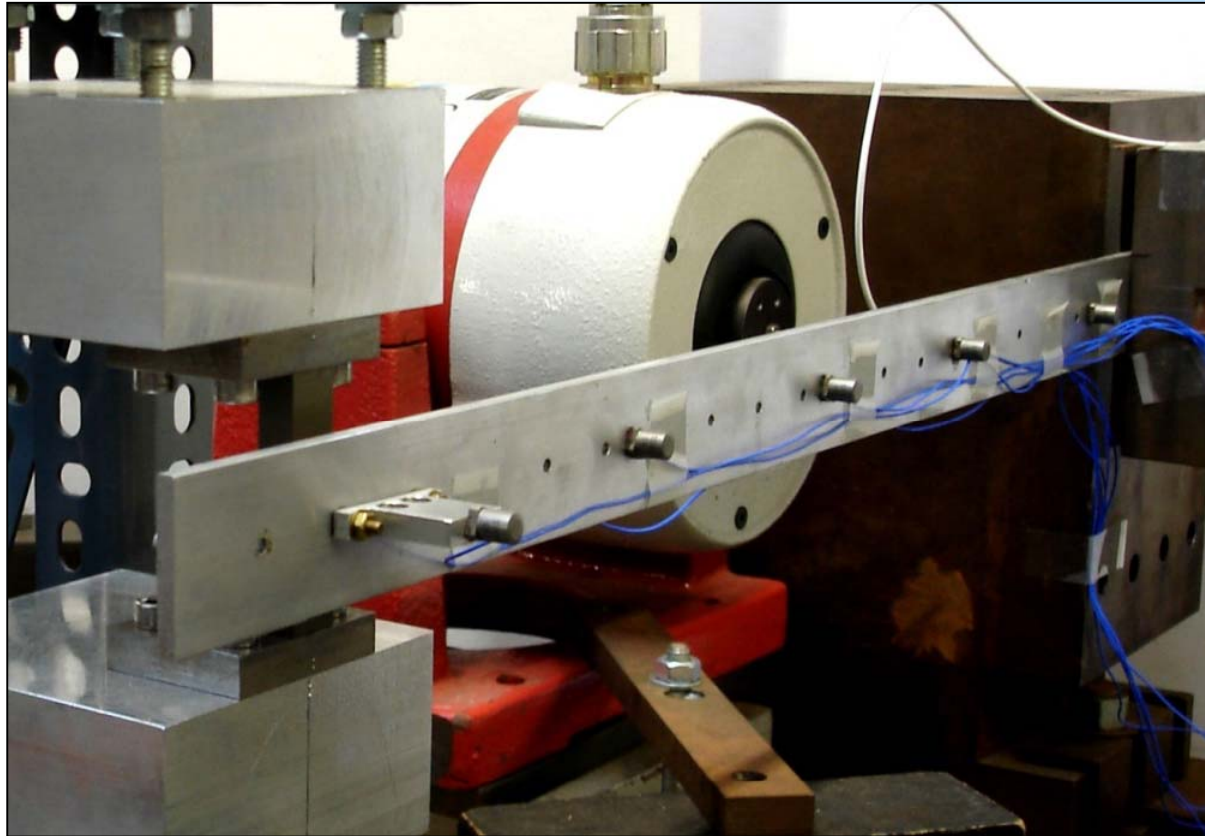
Goland wing



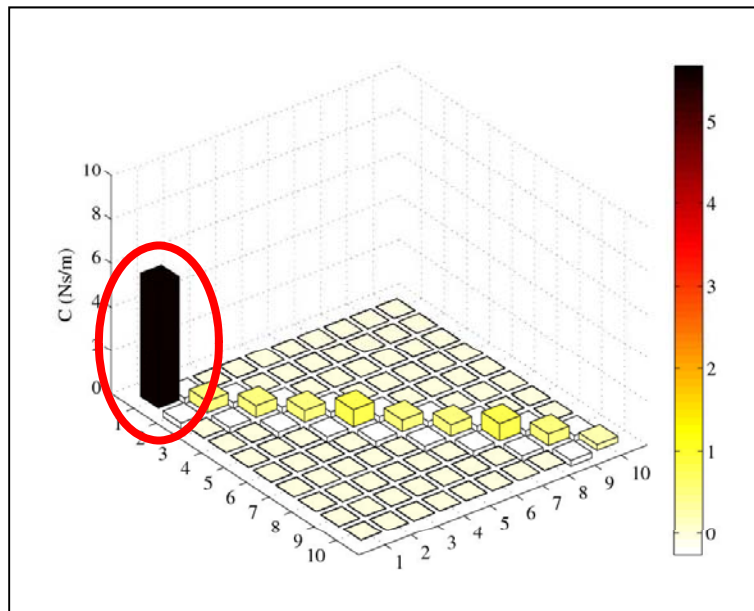
Goland wing simulation



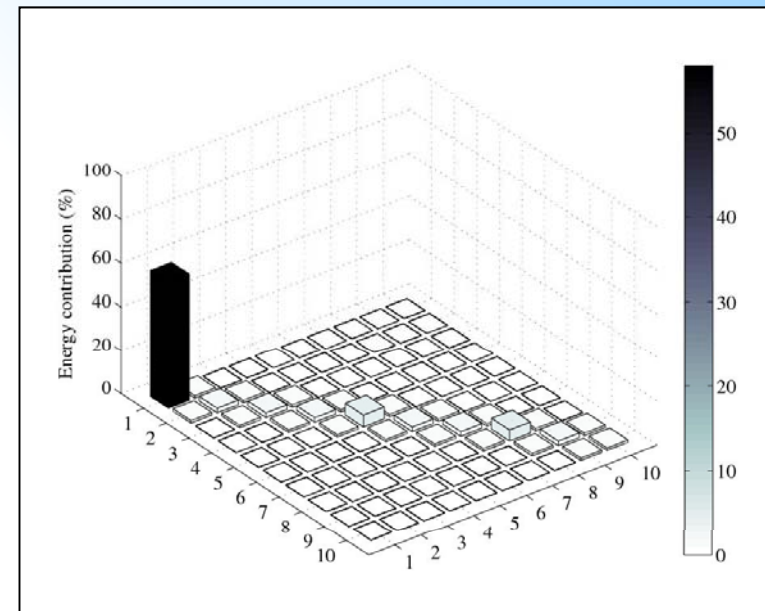
Experiment setup



Undamped system

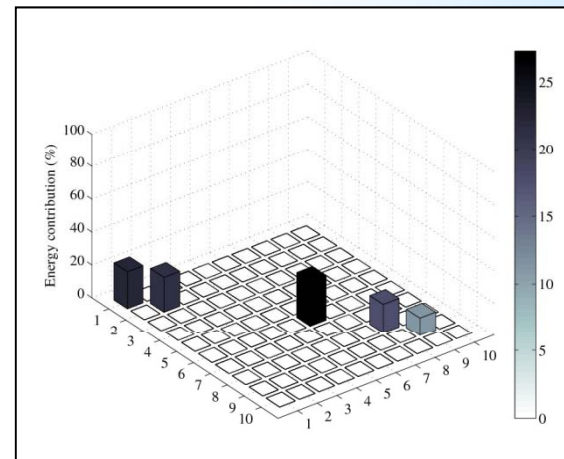
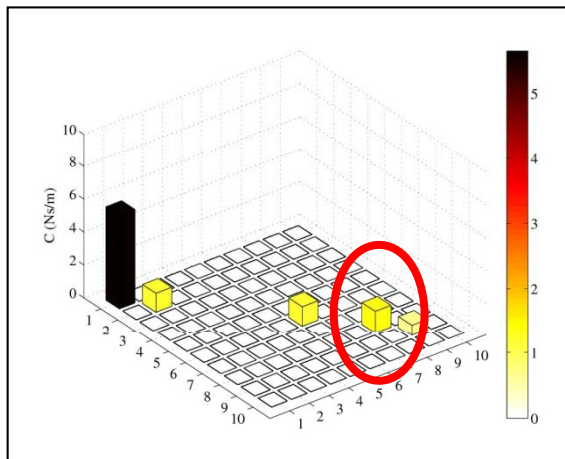
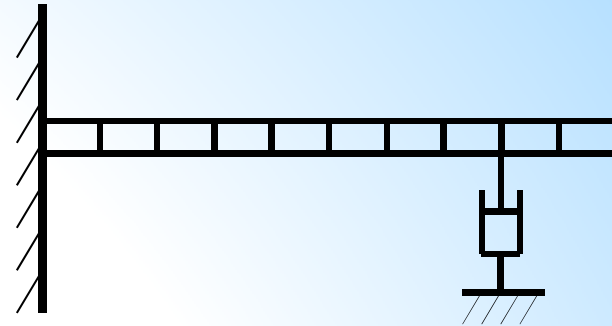
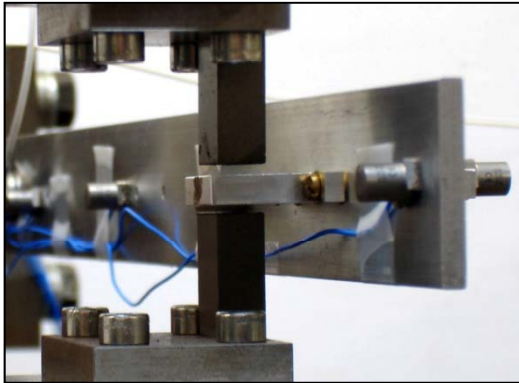


Viscous damping matrix

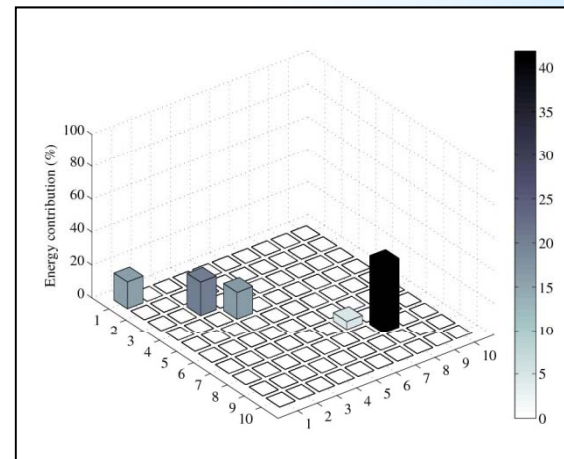
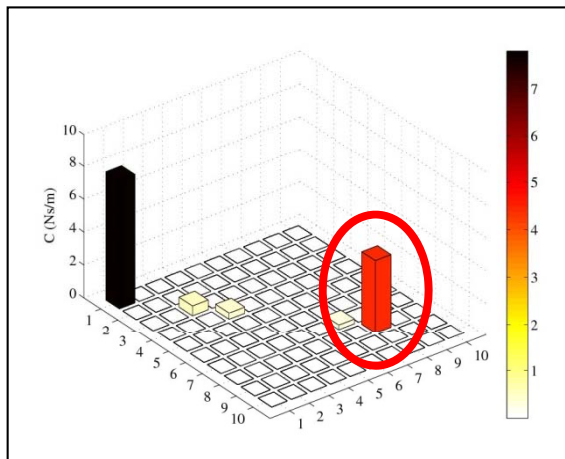
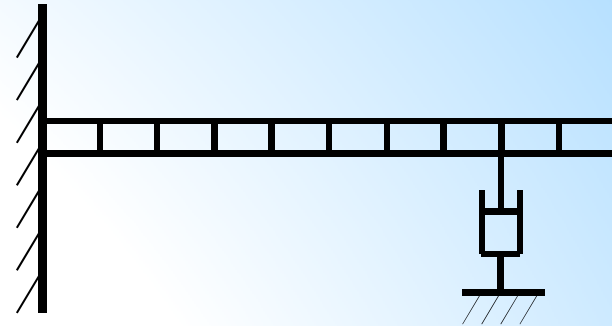
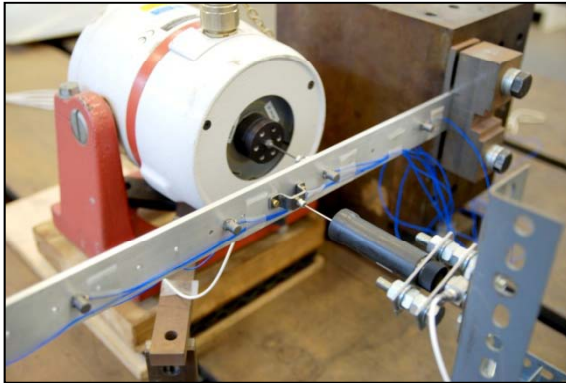


Energy dissipated (%)

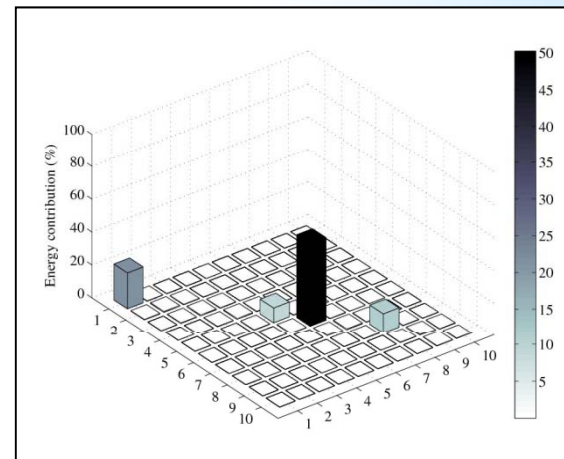
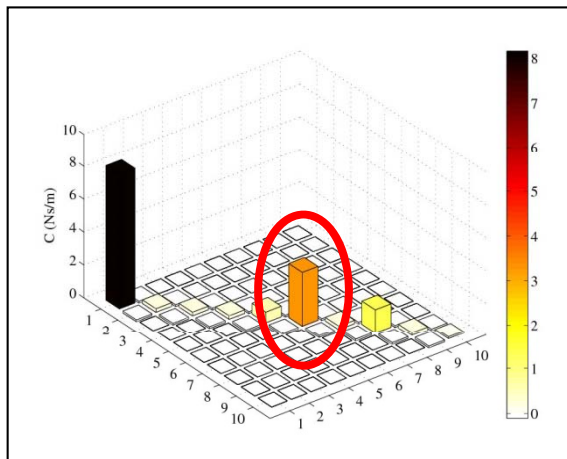
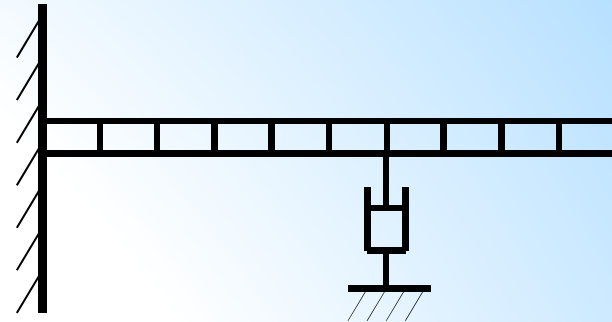
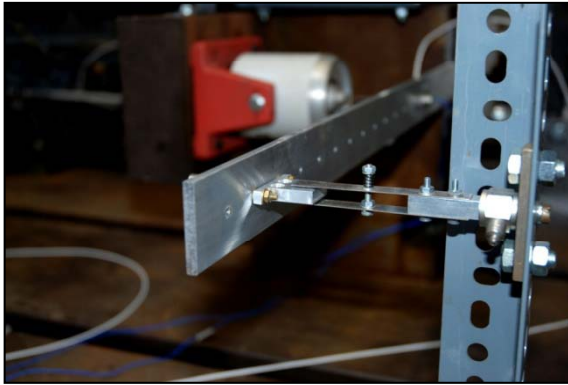
Magnetic damping (DOF 8)



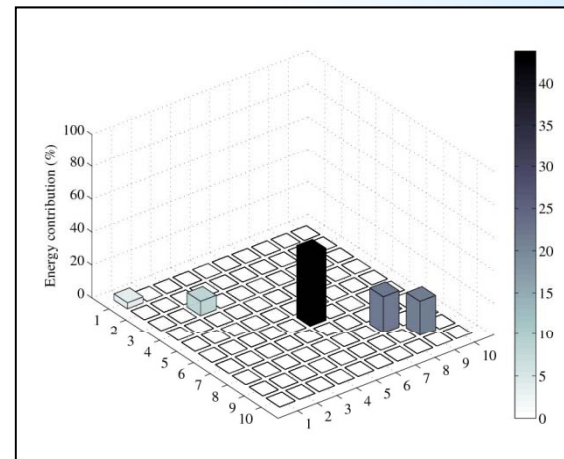
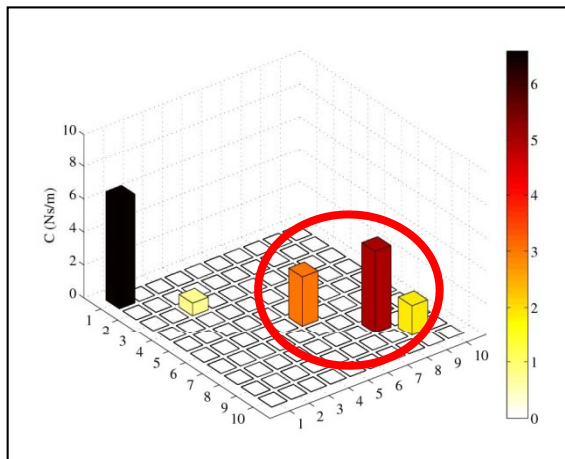
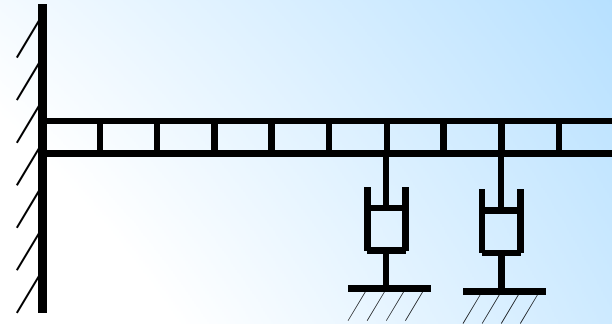
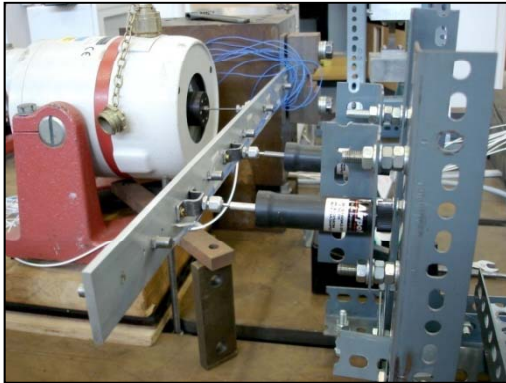
Air dashpot (DOF 8)



Coulomb friction (DOF 6)

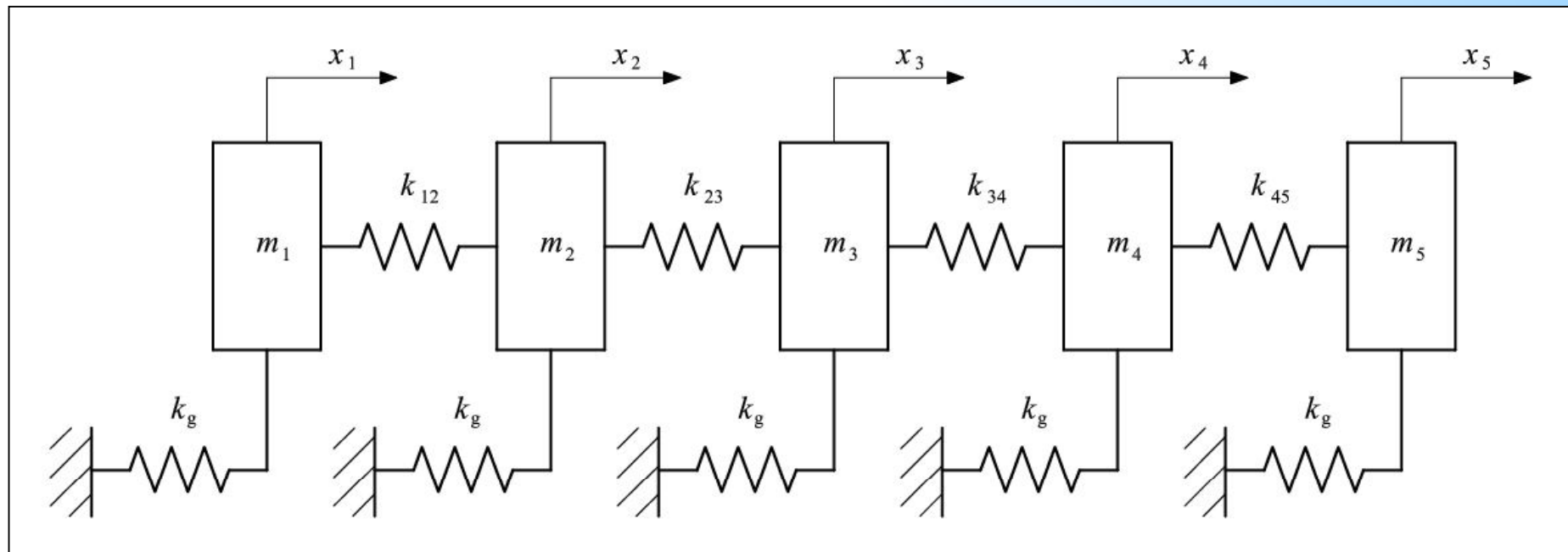


Multiple air dashpots (DOF 6 and 8)



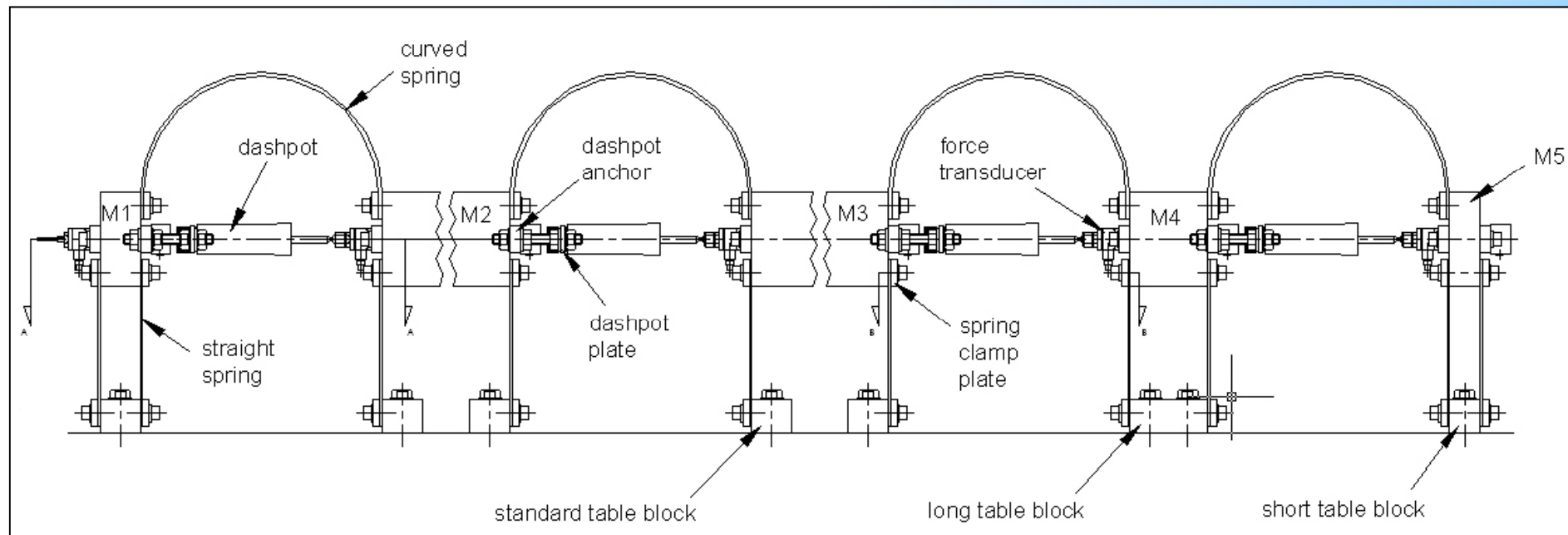
Experiment 2

5-mass system



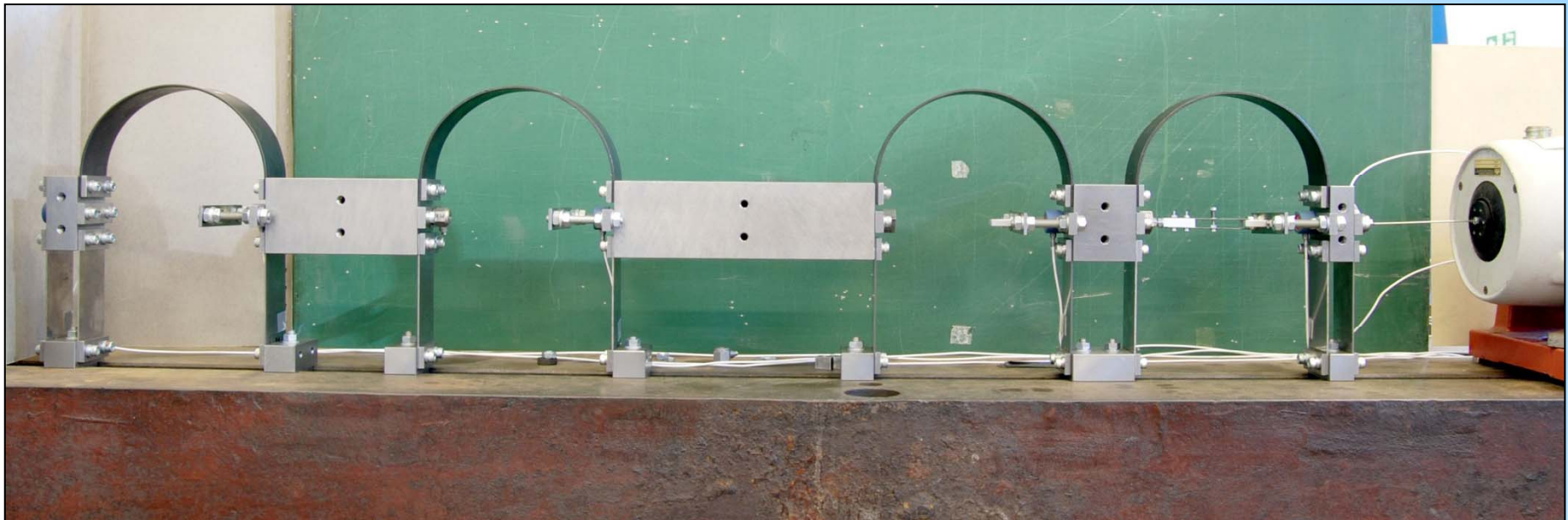
Experiment 2

5-mass system



Experiment 2

5-mass system



Viscous dashpot (DOF 4-5)

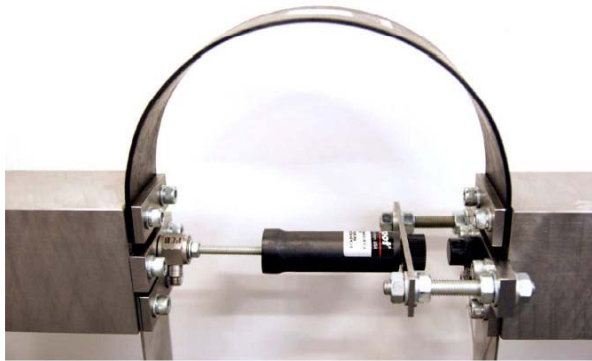


Figure 6.32: Viscous dashpot between DOFs 4 and 5

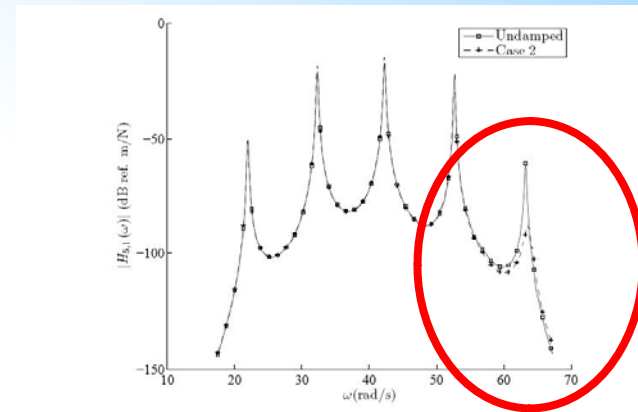


Figure 6.33: Experiment 2: FRF of the undamped system versus case 2

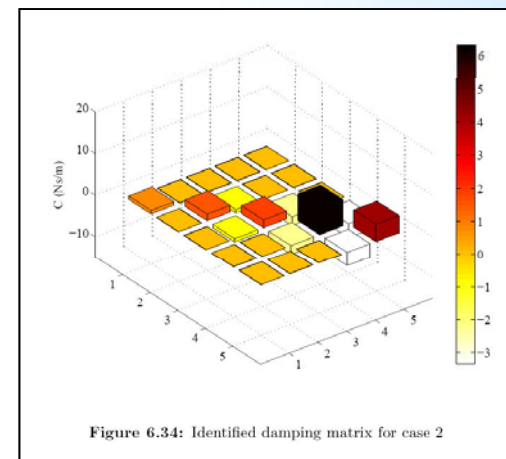
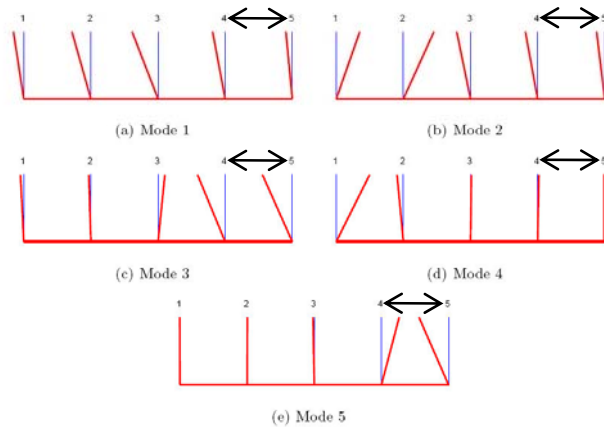


Figure 6.34: Identified damping matrix for case 2

2 dashpots (DOF 2-3 and 4-5)

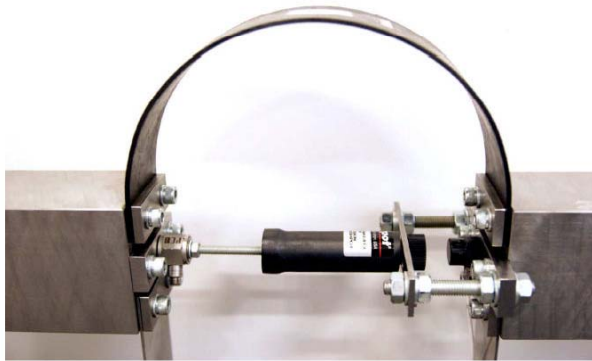


Figure 6.32: Viscous dashpot between DOFs 4 and 5

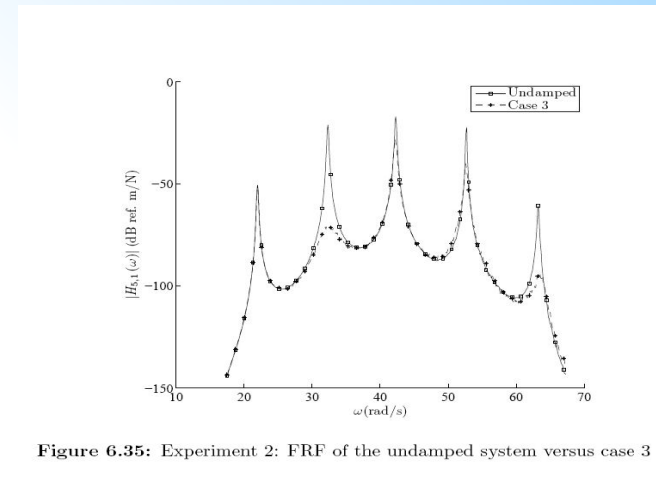


Figure 6.35: Experiment 2: FRF of the undamped system versus case 3

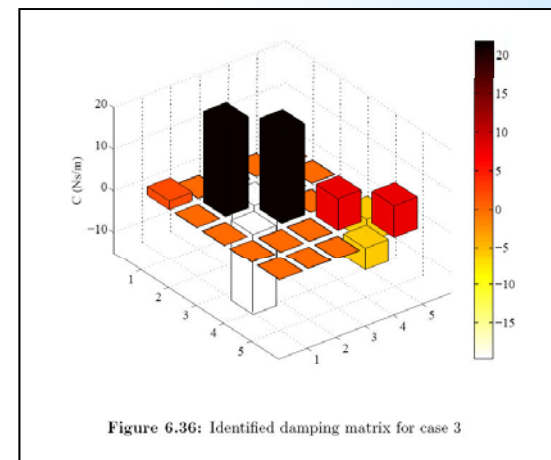
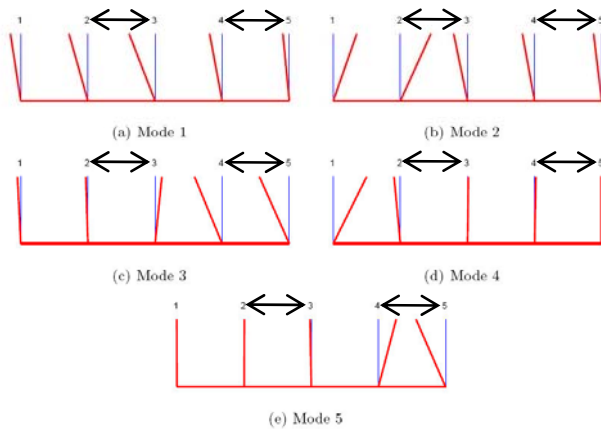


Figure 6.36: Identified damping matrix for case 3

Viscous (DOF 3-4) Coulomb (2-3)

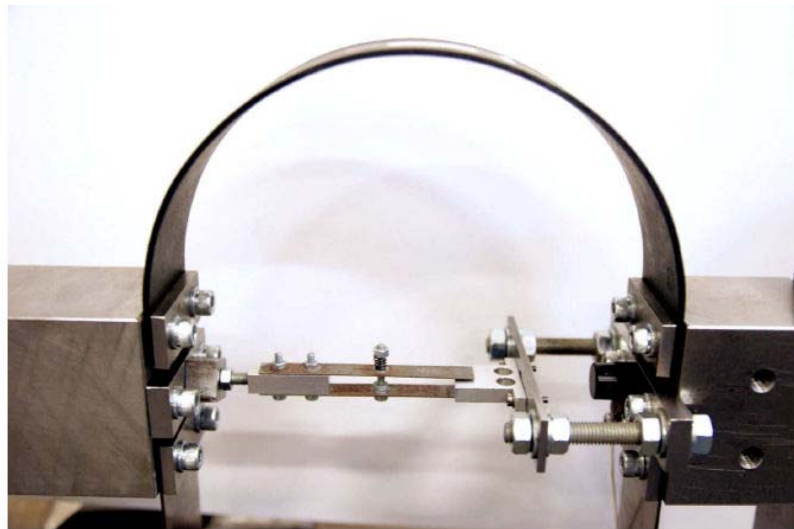


Figure 6.39: Coulomb friction device between DOFs 3 and 4

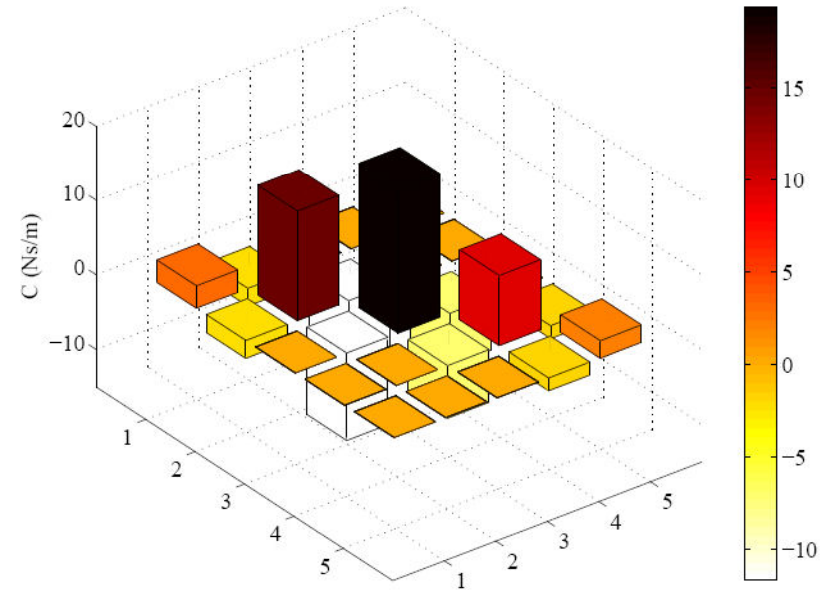


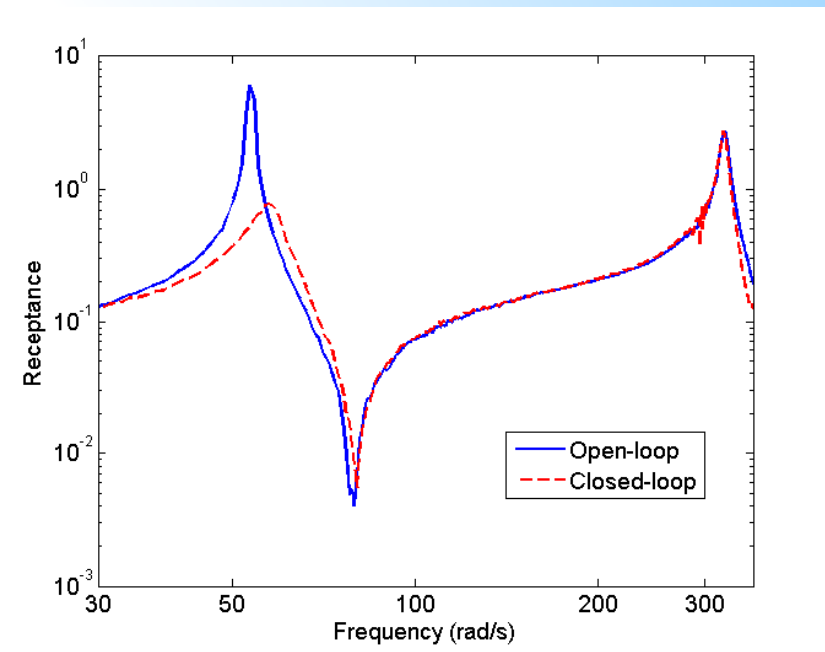
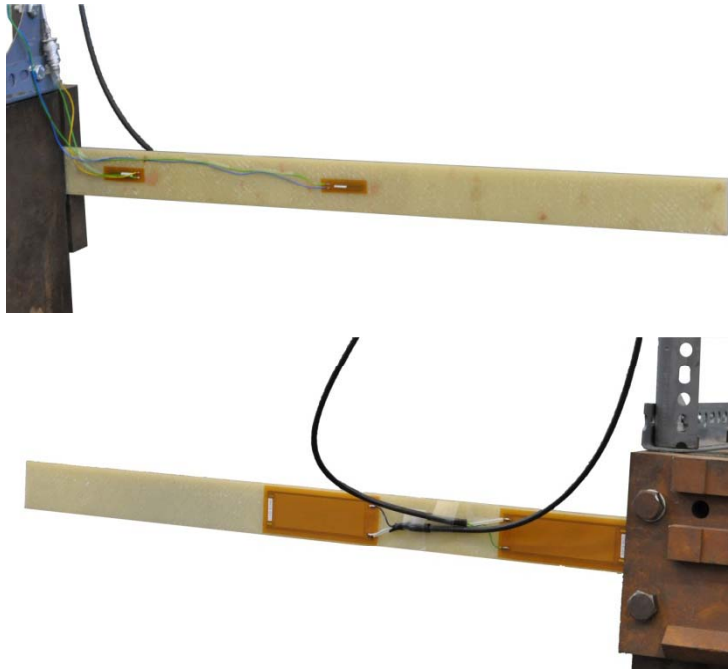
Figure 6.40: Identified damping matrix for case 4

Future work

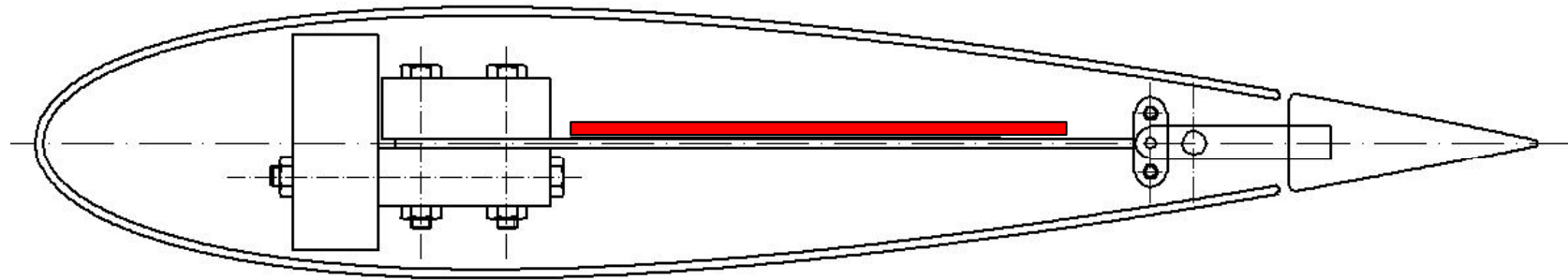
- Further investigation on non-linear damping.
- Updating damping amplitudes by combining modal damping established methods.
- Damage or defect detection.

Current work

Receptance method in active vibration control of an aerofoil using piezoelectric actuators



Current work



Acknowledgements

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- Marie Curie Actions

Thank you